

**Additional Mathematics- 0606****Permutation and combinations answers****1)**

$$(i) \frac{9 \times 8 \times 7 \times 6}{4 \times 3 \times 2 (\times 1)}$$

126

$$(ii) \frac{4 \times 3}{2 (\times 1)}$$

$$\left( \frac{4 \times 3}{2 (\times 1)} \right) \times 3 \times 2$$

36

- (iii) adds number of arrangements of 2,1,1 and 1,2,1 and 1,1,2 only  
 multiplies for each selection  
 $(36) + 4 \times 3 \times 2 + 4 \times 3 (\times 1)$   
 72

**2)**

(i) 40320

$$(ii) \frac{8 \times 7 \times 6 \times 5 \times 4}{5 \times 4 \times 3 \times 2 (\times 1)} \text{ or } \frac{8!}{5! \times 3!}$$

56

- (iii) uses 5, 4 and 3 only  
 60

**3)**

(i)  ${}^7P_4 = 840$

(ii)  $4 \times {}^6P_3$  or  $\frac{4}{7} \times 840$   
 480

4)

(i)  $7 \times 6 \times 5 \times 4$   
840

(ii)  $2 \times 6 \times 5 \times 4$  or  $\frac{2}{7} \times (840)$   
240

(iii)  $2 \times 5 \times 4 \times 2$  or  $\frac{2}{6} \times (240)$  or clear indication of method  
80

5)

(i)  ${}^{14}C_6 = 3003$

(ii)  ${}^8C_4 \times {}^6C_2$   
 $= 1050$

(iii)  ${}^8C_6 + 6{}^8C_5 = 364$

6)

(i) Evidence of 8, 7, 6, 5, 4, 3, 2, 1 or 8!  
40320

(ii) Evidence of 5! (120) or 4! (or 24)  
2880

$$\frac{7 \times 6 \times 5}{3 \times 2(\times 1)} (= 35) \text{ and } \frac{5 \times 4}{2(\times 1)} (= 10)$$

Multiply  
350

7)

(i)  $6! = 720$

(ii)  $2 \times 5! = 240$

(iii)  $4 \times 5! = 480$

(iv) Even first and last:  $4!$  (24)  
Odd first and even last:  $4 \times 4!$  (144)  
Total:  $7 \times 4! = 168$

8)

- (i) Evidence of  $4 \times 3 \times 3 \times 2 \times 2(\times 1 \times 1)$  or  $4 \times 3 \times 3 \times 2 \times 2(\times 1 \times 1)$  or  $4! \times 3!$   
144
- (ii)  $4!$  (or 24) for boys and  $3!$  (or 6) for girls  
288
- (iii) Evidence of  $4 \times (120) \times 3$  or  $(4) \times 5! \times (3)$   
1440

9)

- (i)  $\frac{14 \times 13 \times 12 \times 11 \times 10 \times 9}{6 \times 5 \times 4 \times 3 \times 2 \times 1}$  or  $\frac{14!}{8! \times 6!}$   
3003
- (ii) Both 5 students + 1 teacher and 4 students + 2 teachers  
 $56 \times 6$  or  $70 \times 15$   
1386
- (iii) 30

10)

- (a) (i) 15120  
(ii) 210
- (b) (i) 15504  
(ii)  ${}^{12}C_{10} \times {}^8C_5$   
 $= 3696$
- (iii) 56

**11)**

**(a) (i)** 792

**(ii)** 4W, 3M and 5W, 2M  
 $5 \times 35$  or  $(1) \times 21$   
196

**(b) (i)**  $4 \times 5 \times 4 \times 3$  or  $\frac{2}{3} \times 6 \times 5 \times 4 \times 3$   
240

**(ii)**  $4 \times 4 \times 3 \times 1$  or  $\frac{1}{5} \times (240)$   
48

**12)**

**(i)**  ${}^{15}C_7 = 6435$

**(ii)**  ${}^6C_2 \times {}^9C_5 = 1890$

**(iii)** No women:  ${}^9C_7 = 36$   
 $6435 - 36$   
 $= 6399$

**13)**

**(i)** Evidence of 6, 5, 4, and 3 only  
360

**(ii)** Evidence of  $2 \times 3$  for outside digits  
Evidence of  $4 \times 3$  for inside digits  
72

**14)**

- (a) (i) 3628800  
 (ii) Evidence of  $5!$  (=120) and  $4!$  (=24)  
 Evidence of  $3!$   
 17280
- (b) (i) Evidence of  $\frac{6 \times 5 (\times 4 \times 3)}{(4 \times 3) \times 2 (\times 1)}$  (=15) or  $\frac{5 \times 4}{2 (\times 1)}$  (=10)  
 Multiplies  
 150  
 (ii) No cousins in 30 ways  
 Older cousin only in 60 ways or younger cousin only in 20 ways  
 110  
 (or both cousins in 40 ways B1, subtract from 150 B1 answer 110 B1)

15)

(i)  $6 \times 5 \times 4 \times 3 = 360$  or  ${}^6P_4 = 360$

(ii)

Position	1	2	3	4
Number of ways	5	4	3	1

or  $\frac{1}{6}$  (i) or  ${}^5P_3$  or  ${}^5C_3 \times {}^6C_1$

Number of 4 digit numbers = 60

(iii)

Position	1	2	3	4
Number of ways	3	4	3	1

or  ${}^3P_1 \times {}^4P_2$

Number of 4 digit numbers = 36

16)

- (i)  ${}^{14}C_6 = 3003$   
 (ii)  ${}^5C_3 \times {}^9C_3 = 840$   
 (iii) **Either**  $3003 - {}^9C_6 = 2919$

**Or**

1M + 5W:	$5 \times {}^9C_5 = 630$
2M + 4W:	${}^5C_2 \times {}^9C_4 = 1260$
3M + 3W:	840 (part (ii))
4M + 2W:	${}^5C_4 \times {}^9C_2 = 180$
5M + 1W:	$1 \times {}^9C_1 = 9$
<b>Total:</b>	2919

17)

(a) (i) 360

(ii) 120

(b) (i) 924

(ii) 28

(iii)  $924 - ({}^8C_3 \times {}^4C_3) - ({}^8C_2 \times {}^4C_4)$   
 (i.e.  $924 - 3M\ 3W - 2M\ 4W$ )  
 $924 - 224 - 28$   
 $= 672$

**Or:** 4M 2W  ${}^8C_4 \times {}^4C_2 = 420$

5M 1W  ${}^8C_5 \times {}^4C_1 = 224$

6M  ${}^8C_6 = 28$

**Total** = 672

**18)**

(a) (i) 15120

(ii)  $(5 \times 4) \times (4 \times 3 \times 2)$

480

(b) (i) 5456

(ii)  ${}^{18}C_2 \times 15$

2295

(iii) 5456 – Number of ways only girls get tickets  
 $5456 - 455 = 5001$

<b>Or</b>	1B 2G	1890
	2B 1G	2295
	3B	816
	Total	5001

**19)**

(a) (i) 720

(ii) 240

(iii) Starts with either a 2 or a 4: 48 ways

Does not start with either a 2 or a 4: 96 ways  
(i.e. starts with 1 or 5)

Total = 144

**Alternative 1:**

Ends with a 2, starts with a 1,4 or 5 : 72 ways

Ends with a 4, starts with a 1,2 or 5 : 72 ways

Total = 144

**Alternative 2:**

$$240 - (2 \times 2 \times {}^4P_3) \text{ or } (4 \times {}^4P_3 \times 2) - (2 \times {}^4P_3) \\ = 144$$

**Alternative 3:**

$${}^3P_1 \times {}^4P_3 \times {}^2P_1 \text{ or } 3 \times 4 \times 2 \\ = 144$$

(b) With twins :  ${}^{16}C_4$  (= 1820)

Without twins:  ${}^{16}C_6$  (= 8008)

Total: 9828

**Alternative:**

$${}^{18}C_6 - (2 \times {}^{16}C_5) \\ = 9828$$



- (a) 1 digit even numbers 2  
 2 digit even numbers  $4 \times 2 = 8$   
 3 digit even numbers  $3 \times 3 \times 2 = 18$   
 Total = 28

- (b) (i) 3M 5W = 35  
 4M 4W = 175  
 5M 3W = 210  
 Total = 420

or  ${}^{12}C_8 - 6M 2W - 7M 1W$   
 $495 - 70 - 5 = 420$

- (ii) Oldest man in, oldest woman out and vice-versa

$${}^{10}C_7 \times 2 = 240$$

**Alternative:**

1 man out                      1 woman in  
 6 men                              4 women

$$6M 1W : {}^6C_6 \times {}^4C_1 = 4$$

$$5M 2W : {}^6C_5 \times {}^4C_2 = 36$$

$$4M 3W : {}^6C_4 \times {}^4C_3 = 60$$

$$3M 4W : {}^6C_3 \times {}^4C_4 = 20$$

$$\text{Total} = 120$$

There are 2 identical cases to consider, so  
 240 ways in all.

21)

- (a) (i) 360  
 (ii) 60  
 (iii) 36

- (b) (i)  ${}^8C_5 \times {}^{12}C_5$   
 $56 \times 792 = 44352$

- (ii) 4 places are accounted for  
 Gender no longer 'important'

$$\text{Need } {}^{16}C_6 = 8008$$

Alternative Method

$$({}^6C_6 \times {}^{10}C_0) + ({}^6C_5 \times {}^{10}C_1) + \dots + ({}^6C_0 \times {}^{10}C_6)$$

$$1 + 60 + 675 + 2400 + 3150 + 1512 + 210 = 8008$$

22)

(i)  ${}^{12}C_4 = 495$

(ii)  ${}^7C_2 \times {}^5C_2 = 21 \times 10$   
 $= 210$

(iii) not K and B =  ${}^6C_2 \times {}^4C_1 = 15 \times 4 = 60$   
K and not B =  ${}^6C_1 \times {}^4C_2 = 6 \times 6 = 36$   
 $60 + 36$   
 $96$

OR

K and B =  ${}^6C_1 \times {}^4C_1 = 6 \times 4 = 24$

not K and not B =  ${}^6C_2 \times {}^4C_2 = 15 \times 6 = 90$

$210 - 90 - 24$

$96$

23)

(a) (i) 20160

(ii)  $3 \times {}^6P_4 \times 2$   
 $= 2160$

(iii)  $5 \times 2 \times {}^6P_4$   
 $= 3600$

(b) (i)  ${}^{14}C_4 \times {}^{10}C_4$  or  ${}^{14}C_8 \times {}^8C_4$   
(or numerical or factorial equivalent)  
 $= 210210$

(ii)  ${}^8C_4 \times {}^6C_4$   
 $= 1050$

24)

(a) Permutation because the order matters

(b) (i)  ${}^6C_4 + {}^5C_4 + {}^7C_4$   
55

(ii)  ${}^2C_1 \times {}^6C_1 \times {}^5C_1 \times {}^7C_1$   
420

(iii)  ${}^6C_3 \times {}^2C_1$  or  ${}^2C_2 \times {}^5C_1 \times {}^6C_1$   
summation  
70

25)

(a) (i) 28

(ii) 20160

(iii)  $6 \times (5 \times 4 \times 3)$  or to give 360  
 $6 \times (5 \times 4 \times 3) \times 2$   
= 720

(b) Either  ${}^{10}C_6 - {}^7C_6 = 210 - 7$   
= 203

Or

1W 5M = 63
2W 4M = 105
3W 3M = 35
Total = 203

26)

(a) (i) Number of arrangements with Maths books as one item =  $4!$  or  $4 \times 3!$

or Maths books can be arranged  $2!$  ways and History  $3!$  ways =  $2! \times 3!$

$$2 \times 4! \text{ or } 2 \times 4 \times 3! \text{ or } 4 \times 2 \times 3! = 48$$

(ii)  $5! - 48$  or  $6 \times 2 \times 3!$

$$72$$

(b) (i) 3003

(ii)  $3003 - 6 - 135$

$$2862$$

or

$$2M \ 3W = 720$$

$$3M \ 2W = 1260$$

$$4M \ 1W = 756$$

$$5M = 126$$

$$2862$$

27)

Any one of:

$$\left[ {}^6C_0 \times \right] {}^7C_3 + {}^6C_1 \times {}^7C_2$$

$$\text{or } 35 + 126$$

$$\text{or } {}^{13}C_3 - {}^6C_2 \times {}^7C_1 - {}^6C_3$$

$$\text{or } 286 - 105 - 20$$

161

28)

- (a) (i)  $2 \times 4!$  or  $\frac{2}{5} \times 5!$  oe  
48
- (ii)  ${}^5P_3$  or  $\frac{5!}{2!}$  or  $5 \times 4 \times 3$  oe  
60
- (b) (i)  $4 \times 2[!] \times 3$  oe  
24
- (ii)  $3!$  or  $3 \times 3$  seen  
18

29)

- (i) Free choice : no. of ways  
 ${}^6C_4 \times {}^5C_2 = 15 \times 10$   
 $= 150$
- (ii) Both Mr and Mrs Coldicott  
 ${}^5C_3 \times {}^4C_1 = 10 \times 4$   
 $= 40$
- (iii) Mr C and not Mrs C  ${}^5C_3 \times {}^4C_2 (= 60)$   
Not Mr C and Mrs C  ${}^5C_4 \times {}^4C_1 (= 20)$   
Total = 80
- OR  
Total = (i) – (ii) – neither  
Neither =  ${}^5C_4 \times {}^4C_2 = 30$   
Total =  $150 - 40 - 30 = 80$

30)

(a) (i)  ${}^{18}C_5 = 8568$

(ii) **Either**

$${}^{10}C_4 \times {}^8C_1 = 1680$$

$${}^{10}C_3 \times {}^8C_2 = 3360$$

$${}^{10}C_2 \times {}^8C_3 = 2520$$

$${}^{10}C_1 \times {}^8C_4 = 700$$

$$\text{Total} = 8260$$

**Or**

$$\text{their } {}^{18}C_5 - ({}^{10}C_5 + {}^8C_5)$$

$$8568 - (252 + 56)$$

$$\text{Total} = 8260$$

(b) (i)  ${}^{10}P_6 = 151200$

(ii)  $4 \times {}^8P_4 \times 3$   
 $= 20160$

(iii) Answer to (i) -  ${}^7P_6$   
 $= 146160$

**Alternative:**

$$1 \text{ symbol: } 45360$$

$$2 \text{ symbols: } 75600$$

$$3 \text{ symbols: } 25200$$

$$\text{Total: } 146160$$

31)

(a)(i)	2520
(a)(ii)	360
(a)(iii)	1080
(a)(iv)	6 or 8 to start with No of ways = $2 \times 5 \times 4 \times 3 \times 2$ = 240
	9 to start with No of ways = $1 \times 5 \times 4 \times 3 \times 3$ = 180
	Total number of ways = 420
(a)(iv)	<b>Alternative 1</b> All numbers > 6000 – all odd numbers > 6000
	1080 – 180 – 480
	Total number of ways = 420
	<b>Alternative 2</b> Even numbers > 60000 : Odd numbers > 60000 7 : 11
	Total number of ways = $\frac{7}{18} \times 1080$
	= 420
(b)(i)	480700
(b)(ii)	26460
(b)(iii)	With brother and sister ${}^{23}C_5 = 33649$
	Without brother and sister ${}^{23}C_7 = 245157$
	Total number of ways = 278806

32)

(a)	$(9 \times 8 \times 7 \times 6 \times 1) + (8 \times 8 \times 7 \times 6 \times 1)$ soi
	5712
(b)	${}^9C_4 \times {}^5C_4 + {}^9C_3 \times {}^5C_5$ oe
	$[630 + 84 = ] 714$

33)

(a)	$[{}^{30}P_2 = ] 870$
(b)(i)	${}^2C_1 \times {}^{14}C_{10}$ oe $(2 \times 1001)$
	2002
(b)(ii)	$({}^2C_1 \times {}^5C_4 \times {}^9C_6) + ({}^2C_1 \times {}^5C_5 \times {}^9C_5)$ oe $(840 + 252)$
	${}^2C_1 \times {}^{14}C_{10}$ - or $({}^2C_1 \times {}^5C_1 \times {}^9C_9 + {}^2C_1 \times {}^5C_2 \times {}^9C_8 + {}^2C_1 \times {}^5C_3 \times {}^9C_7)$ $\{2002 - (10 + 80 + 720)\}$
	1092

34)



(a)(i)	${}^8C_6 \times {}^6C_4$	B1
	420	B1
(a)(ii)	${}^{12}C_8 + {}^{12}C_{10}$	B2
	= 561	B1
	Alternate scheme: $1001 - (2 \times {}^{12}C_9)$	B1 B1
	= 561	B1
(b)(i)	136080	B1
(b)(ii)	No of ways ending with 0 - 15 120	B1
	No of ways ending with 5 - 13 440	B1
	Total 28 560	B1
(b)(iii)	Starting with 6 or 8 - 13 440	B1
	Starting with 7 or 9 - 16 800	B1
	Total = 30 240	B1

**35)**

(a)(i)	720	B1
(a)(ii)	240	B1
(a)(iii)	$k \times 4! \times 2$ or $240 - k \times 4! \times 2$ or correct equivalents with no extra terms added or subtracted	B1
	$4 \times 4! \times p$ or correct equivalents with no extra terms added or subtracted	B1
	192	B1
(b)(i)	6435	B1
(b)(ii)	With twins: ${}^{13}C_6$ or 1716 Without twins: ${}^{13}C_8$ or 1287	B2
	Total: $1716 + 1287 = 3003$	B1

36)

(i)	${}^{10}C_4 = 210$	B1
(ii)	2 Mystery 2 others = ${}^5C_2 \times {}^5C_2 = 100$	B3
	3 Mystery 1 other = ${}^5C_3 \times {}^5C_1 = 50$	
	4 Mystery = ${}^5C_4 = 5$	
	Total 155	
(ii)	<u>Alternative Method</u>	
	All – 0 Mystery – 1 Mystery	B1
	= $210 - {}^5C_4 - {}^5C_1 \times {}^5C_3$	B1
	= $210 - 5 - 5 \times 10 = 155$	B1
(iii)	2M1C1R = ${}^5C_2 \times {}^3C_1 \times {}^2C_1 = 60$ 1M2C1R = ${}^5C_1 \times {}^3C_2 \times {}^2C_1 = 30$ 1M1C2R = ${}^5C_1 \times {}^3C_1 \times {}^2C_2 = 15$ Total 105	B3

37)

(i)	$({}^{12}P_7 = ) 3991680$	B1	
(ii)	$(4 \times {}^{11}P_6 = ) 1330560$	B1	
(iii)	$4! \times 4! \times 2$ oe	M2	M1 for $4! \times 4!$ oe only or ${}^4P_4 \times {}^4P_3$ oe only
	1152	A1	

38)

(a)	${}^7P_4$ or $7 \times 6 \times 5 \times 4$ oe	M1	
	840	A1	
(b)(i)	20	B1	
(b)(ii)	${}^5C_1 \times {}^4C_1 \times {}^2C_1$ or $5 \times 4 \times 2$ oe	M1	
	40	A1	
(b)(iii)	${}^5C_3 + {}^4C_3$ oe	M1	
	14	A1	

39)

(i)	120	2	B2 $5 \times 4 \times 3 \times 2$ or B1 for pattern $n(n-1)(n-2)(n-3)$
(ii)	720	2	B1 $4 \times 3 \times 2$ B1 dep $\times 6 \times 5 = 720$
(iii)	2520	2	B1 $4 \times \dots \times \dots \times \dots \times 3$ B1 Dep $\times 7 \times 6 \times 5 = 2520$

40)

(a)	Number first $= 7 \times 6 \times 5 \times 6 \times 5$ or ${}^7P_3 \times {}^6P_2$ or 6300	B1	
	Letter first $= 6 \times 5 \times 4 \times 7 \times 6$ or ${}^6P_3 \times {}^7P_2$ or 5040	B1	
	$6300 + 5040 = 11\,340$	B1	
(b)	With 2 sisters $= {}^7C_5 \times {}^3C_2 = 63$ With 1 sister $= {}^7C_6 \times {}^3C_1 = 21$ With no sister $= {}^7C_7 = 1$ and Total 85	3	B1 One combination evaluated B1 Another combination evaluated B1 Third combination and 85
	OR		
	Total no of ways $= {}^{10}C_7 = 120$	B1	
	With 3 sisters $= {}^7C_4 = 35$	B1	
	Without 3 sisters $= 120 - 35 = 85$	B1	

41)

(i)	167 960	1	
(ii)	evidence of selecting from 16	M1	
	$[{}^{16}C_7 = ] 11\,440$	A1	
(iii)	$2 \times {}^n C_r$ with $n = 16$ or $r = 9$	M1	
	$[2 \times {}^{16}C_9 = ] 22880$	A1	
(iv)	$4 \times {}^n C_r$ with $n = 16$ or $r = 9$	M1	
	$[4 \times {}^{16}C_9 = ] 45760$	A1	

42)

Total IGCSE Revision

(a)(i)	40320	<b>B1</b>	
(a)(ii)	No. of ways with maths books as 1 unit = $5!$ or $5 \times 4!$ or ${}^5P_5$ or 120	<b>B1</b>	
	No. of ways maths books can be arranged amongst themselves = $4!$ or ${}^4P_4$ or 24	<b>B1</b>	
	Total = $(5! \times 4! \text{ oe}) = 2880$	<b>B1</b>	
(a)(iii)	No. of ways with maths books as 1 unit and geography books as 1 unit = $3!$ or ${}^3P_3$ or $3 \times 2!$ or 6	<b>B1</b>	
	No. of ways maths books can be arranged amongst themselves and geography books can be arranged amongst themselves = $4! \times 3!$ or ${}^4P_4 \times {}^3P_3$ or 144	<b>B1</b>	
	Total = $(3! \times 4! \times 3! \text{ oe})$ = 864	<b>B1</b>	
(b)(i)	${}^{12}C_6 = 924$	<b>B1</b>	
(b)(ii)	<b>Either:</b> $924 - {}^8C_6$	<b>M1</b>	For <i>their (i)</i> – the number of teams of just men
	Total = 896	<b>A1</b>	
	<b>Or:</b> $5M\ 1W : {}^8C_5 \times {}^4C_1 \quad (= 224)$ $4M\ 2W : {}^8C_4 \times {}^4C_2 \quad (= 420)$ $3M\ 3W : {}^8C_3 \times {}^4C_3 \quad (= 224)$ $2M\ 4W : {}^8C_2 \times {}^4C_4 \quad (= 28)$	<b>M1</b>	For a complete method
	Total = 896	<b>A1</b>	

43)

(a)(i)	$7! = 5040$	<b>B1</b>	
(a)(ii)	Treating the 4 trophies as 1 unit so there are $4!$ ways	<b>B1</b>	Maybe implied by a correct answer
	There are also $4!$ ways of arranging the football trophies amongst themselves	<b>B1</b>	
	Total = $4! \times 4! = 576$	<b>B1</b>	
(a)(iii)	Treating the 4 football trophies as 1 unit and the 2 cricket trophies as 1 unit so there are $3!$ ways	<b>B1</b>	Maybe implied by a correct answer
	There are also $4!$ ways of arranging the football trophies amongst themselves and 2 ways of arranging the cricket trophies	<b>B1</b>	Maybe implied by a correct answer
	Total = $3! \times 4! \times 2 = 288$	<b>B1</b>	
(b)(i)	3003	<b>B1</b>	
(b)(ii)	28	<b>B1</b>	
(b)(iii)	$3003 - 1$	<b>M1</b>	For <i>their (i)</i> - 1
	3002	<b>A1</b>	<b>FT</b>

44)

(a)(i)	39 916 800	<b>B1</b>	
(a)(ii)	$5! \times 6!$ oe	<b>M1</b>	
	86 400	<b>A1</b>	
(b)(i)	${}^5C_3 \times {}^3C_1$ oe	<b>M1</b>	
	30	<b>A1</b>	
(b)(ii)	${}^5C_2 \times {}^3C_2 + {}^5C_1 \times {}^3C_1$ oe	<b>M1</b>	
	45	<b>A1</b>	

45)

(a)(i)	362 880	<b>B1</b>	
(a)(ii)	$7! \times 2$	<b>B1</b>	For 7!
	10 080	<b>B1</b>	For $7! \times 2$ leading to 10080
(a)(iii)	Total = $4! \times 4! \times 3! = 3456$	<b>B3</b>	<b>B1</b> for treating as 4 separate units 4! <b>B1</b> for either number of ways of arranging the maths books amongst themselves 4! or the number of ways of arranging the physics books amongst themselves 3!
(b)(i)	18 564	<b>B1</b>	
(b)(ii)	Total 3738	<b>B4</b>	<b>B1</b> 4 boys 3150 <b>B1</b> 5 boys 560 <b>B1</b> 6 boys 28

46)

(i)	${}^{14}P_5$ or $14 \times 13 \times 12 \times 11 \times 10$	<b>M1</b>	
	240 240	<b>A1</b>	cao
(ii)	${}^3P_1 \times {}^5P_2 \times {}^6P_2$ or $3 \times (5 \times 4) \times (6 \times 5)$	<b>M1</b>	Two of the three elements multiplied by ...
	= 1800	<b>A1</b>	
(iii)	${}^6P_2 \times {}^8P_3$ or $(6 \times 5) \times (8 \times 7 \times 6)$	<b>M1</b>	One element multiplied by ... Clear intention to multiply
	= 10 080	<b>A1</b>	

47)

(i) 362880 (363000)
(ii) PG or GP in $8! \times 2 = 80640$ or $7/9$ of (i)  $362880 - 80640 = 282240$
(iii) ${}^9P_3$ or ${}^9C_3 \times 3!$ or $9!/6!$  = 504
(iv) ${}^8C_2 \times 3!$ or $504 - {}^8C_3 \times 3!$ or ${}^8P_2 \times 3$  = 168
(v) PG and $x$ in $7 \times 2 \times 2$ ways = 28  Answer $504 - 28 = 476$

48)

(a)(i)	15 120	<b>B1</b>	
(a)(ii)	1680	<b>B1</b>	
(a)(iii) Method 1	Total = 2310	<b>B3</b>	B1 1st digit is 7 or 9    1680 or $210 \times 8$ B1 1st digit is 8        630 or $210 \times 3$
(a)(iii) Method 2	Total = 2310	<b>B3</b>	B1 for 5 <sup>th</sup> digit is 2,4 or 6    1890 or $210 \times 9$ B1 for 5 <sup>th</sup> digit is 8        420 or $210 \times 2$
(b)(i)	3003	<b>B1</b>	
(b)(ii)	28	<b>B1</b>	
(b)(iii)	Total 1419	<b>B3</b>	B1 Including husband and wife    495 B1 Excluding husband and wife    924